

Implementation of an RTZ code for feedback DAC on a Sigma-Delta modulator

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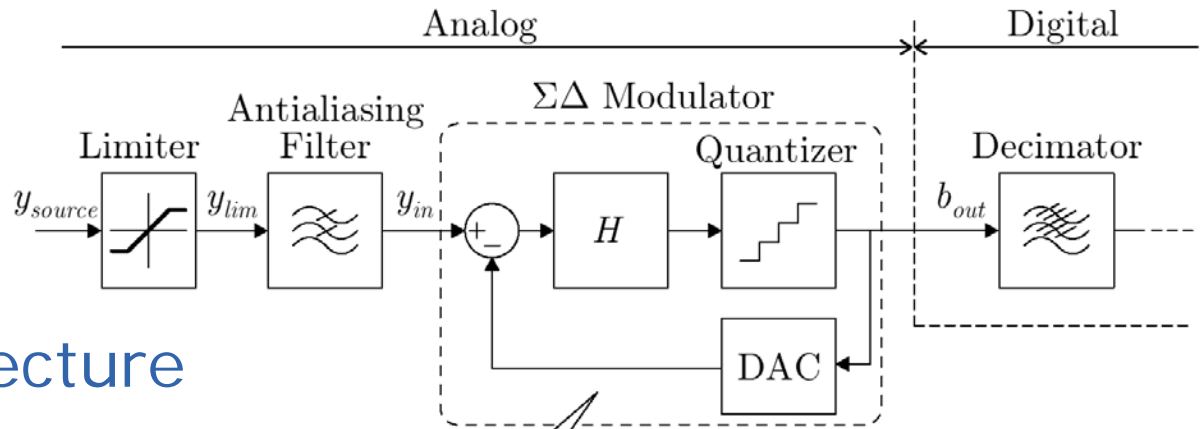
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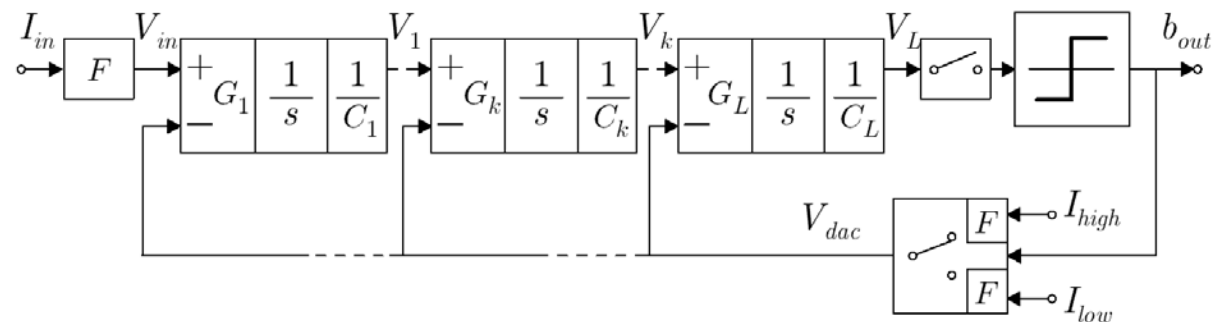
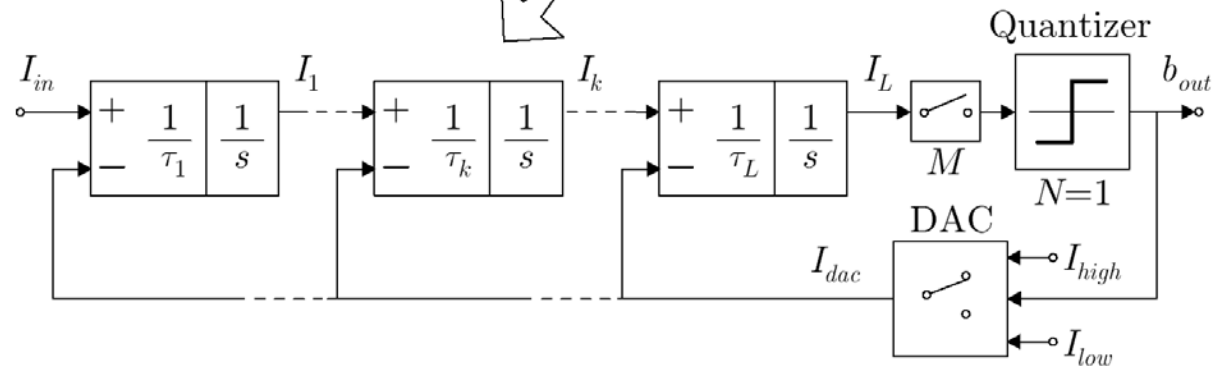
- 1 Introduction
- 2 Waveform Assymetry Modelling
- 3 RTZ code consequences
- 4 Conclusions

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$\Sigma\Delta$ modulator architecture

- ▶ Continuous-time
- ▶ Single-loop
- ▶ 1-bit quantizer
- ▶ Log-domain



CMOS Log-Domain

- ✓ Very low-voltage
- ✓ Low-power
- ✓ MOS-only
- ✓ EKV equations

Simulation Issues

- ✗ High-accuracy
- ✗ Continuous-time
- ✗ Oversampling
- ✗ Pseudo-periodic

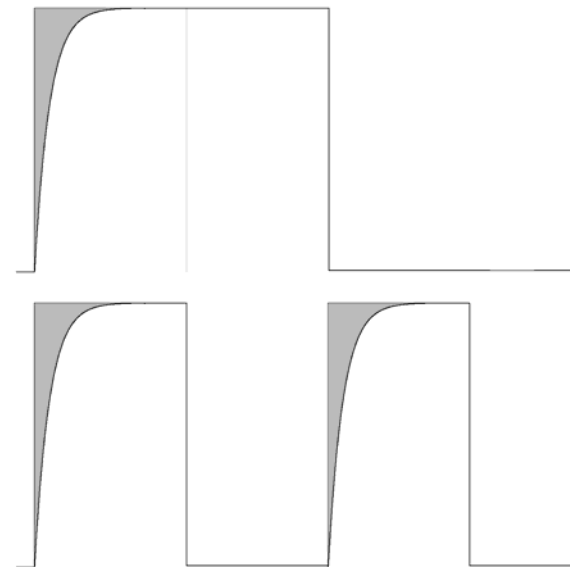
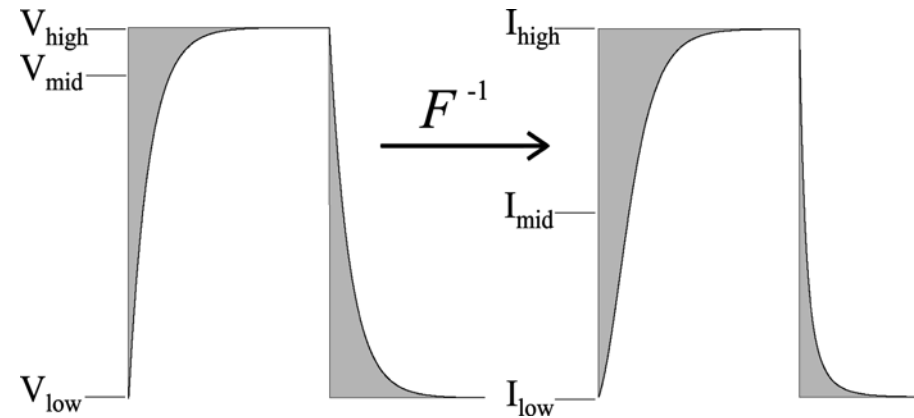
. . . need for high-level analytical modeling!

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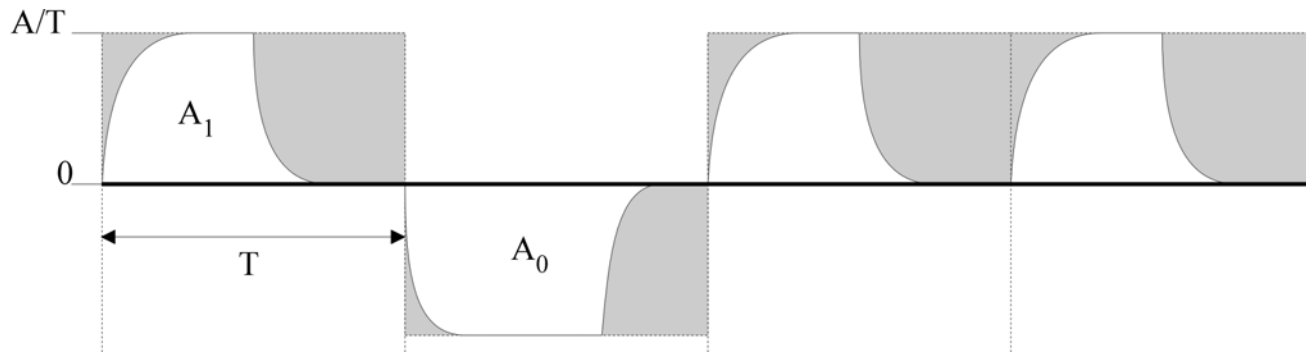
Waveform Asymmetry

- ▶ Waveform asymmetry is enlarged due to log domain operation
- ▶ Integration error exhibits code dependency
- ▶ Error power spectral density is plain inside signal band
- ▶ Error differences must be below 0.5% to achieve 12 bits!

. . . need for another
feedback code!
→ RTZ coding





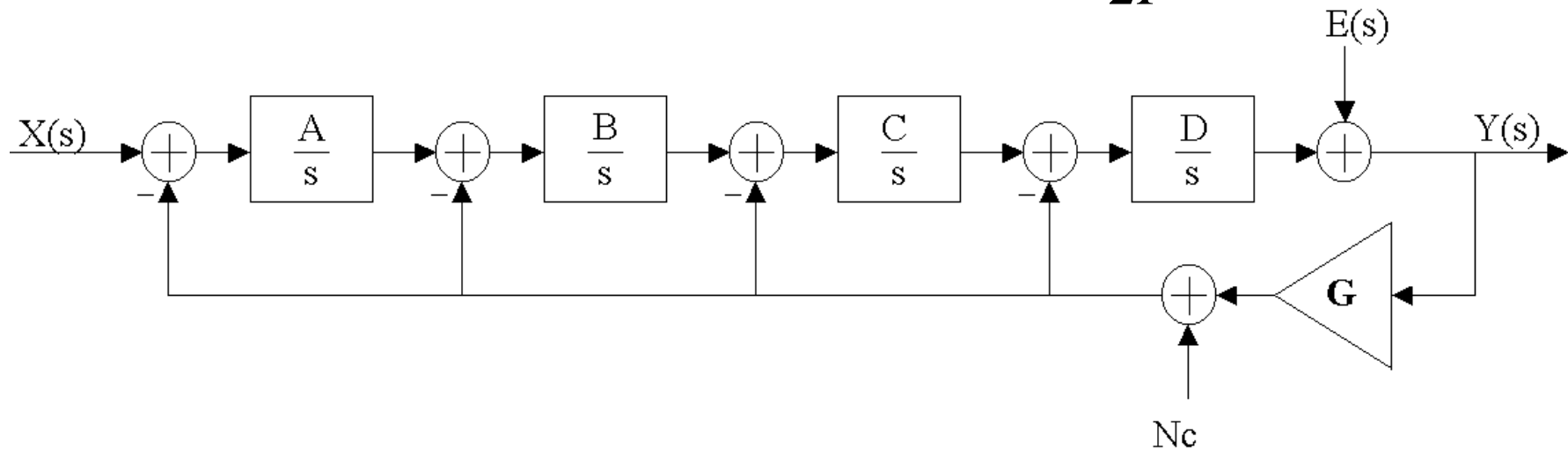


Easy parameter extraction

- ▶ Based on bit-area differences
- ▶ Extracted from short transient electrical simulations

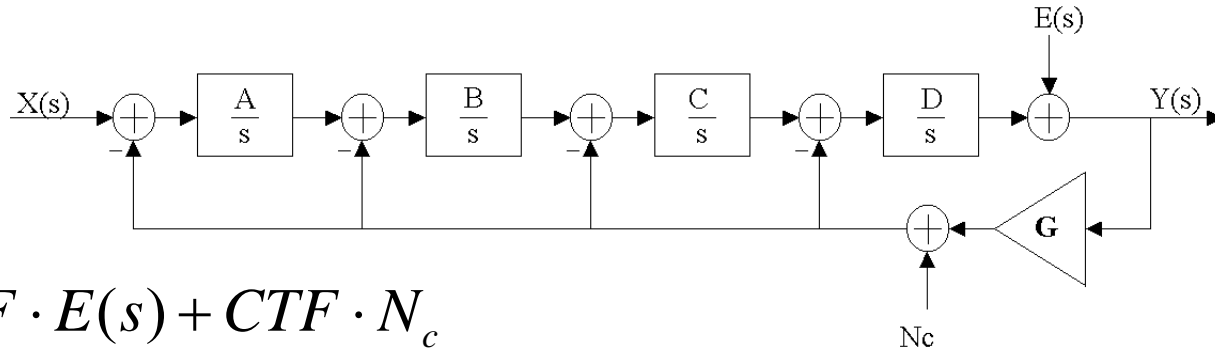
$$G = 1 - P = \frac{A_1 + A_0}{2A}$$

$$N_C = \frac{A_1 - A_0}{2T}$$



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Changes in transfer functions

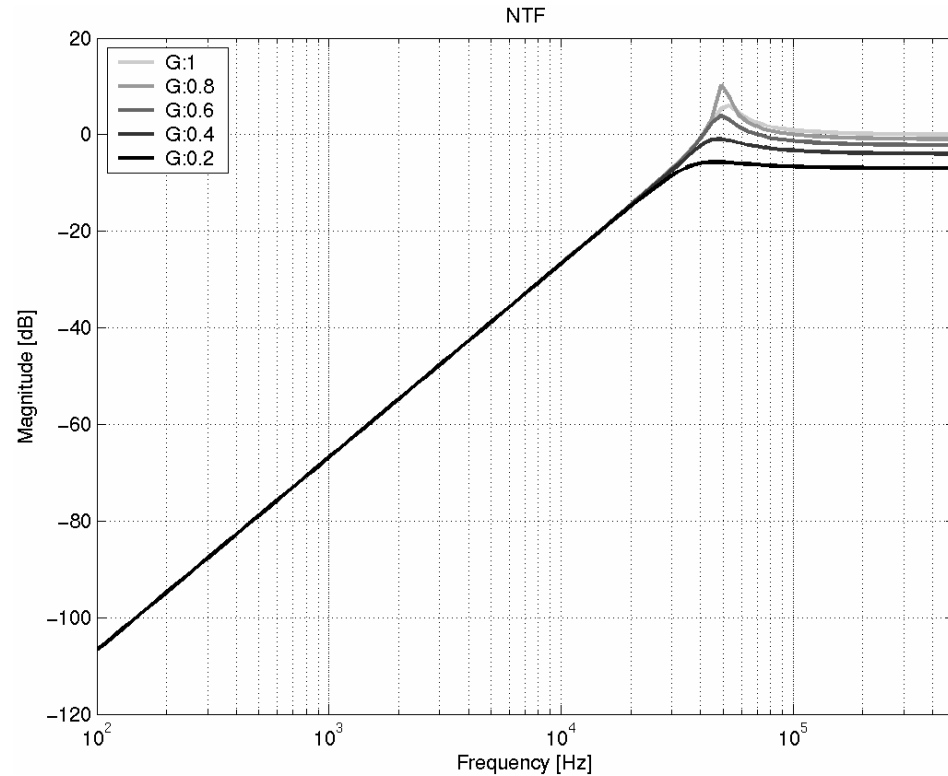


$$Y(s) = STF \cdot X(s) + NTF \cdot E(s) + CTF \cdot N_c$$

► A G reduction on feedback, can be viewed as a $1/G$ amplification on signal

$$STF \approx 1/G \quad CTF \approx -1/G$$

► NTF doesn't changes inside signal band (Quantization error $E(s)$ is reduced by G)



$$NTF = \frac{s^4}{s^4 + G D s^3 + G C D s^2 + G B C D s + G A B C D}$$

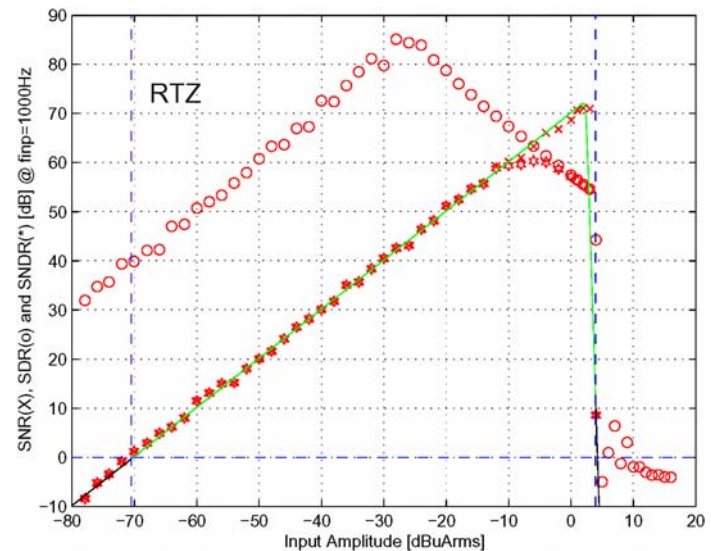
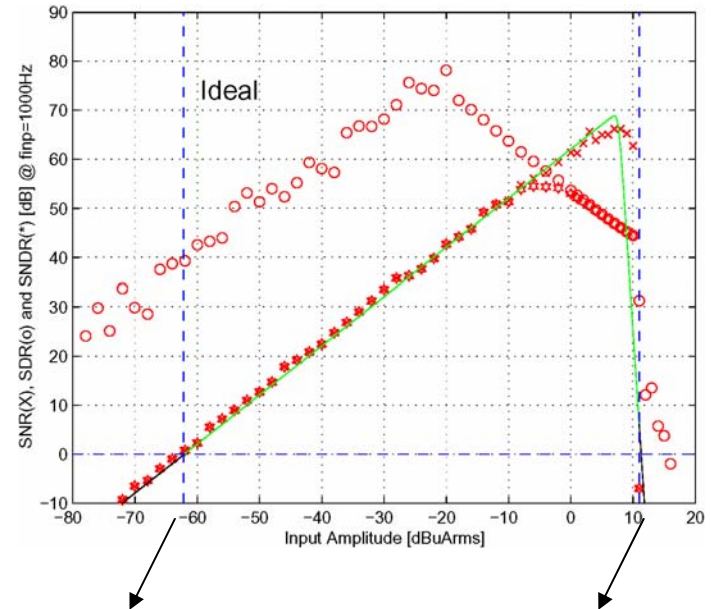
Changes in overall performance

► I_{max} reduction

$$|I'_{max}| = \frac{|I'_{max}| + |N_c|}{G} \Rightarrow |I'_{max}| = G|I_{max}| - |N_c|$$

► DR displacement

- If quantization error is the main source of noise, a decrease on RTZ cycle produces a DR left-shift.
- A dynamically changed RTZ duty cycle allows us to work on best SNR point and expands DR.



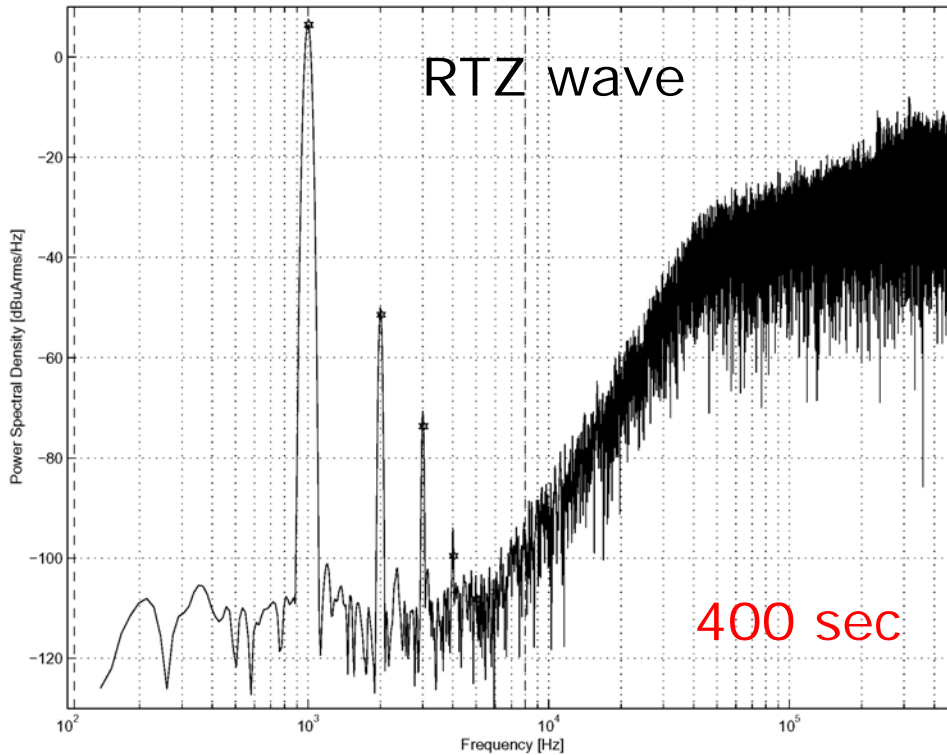
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High-level simulations

- ▶ $G+N_c$ model matches RTZ simulation
- ▶ Simulation speed improvement > 10 times

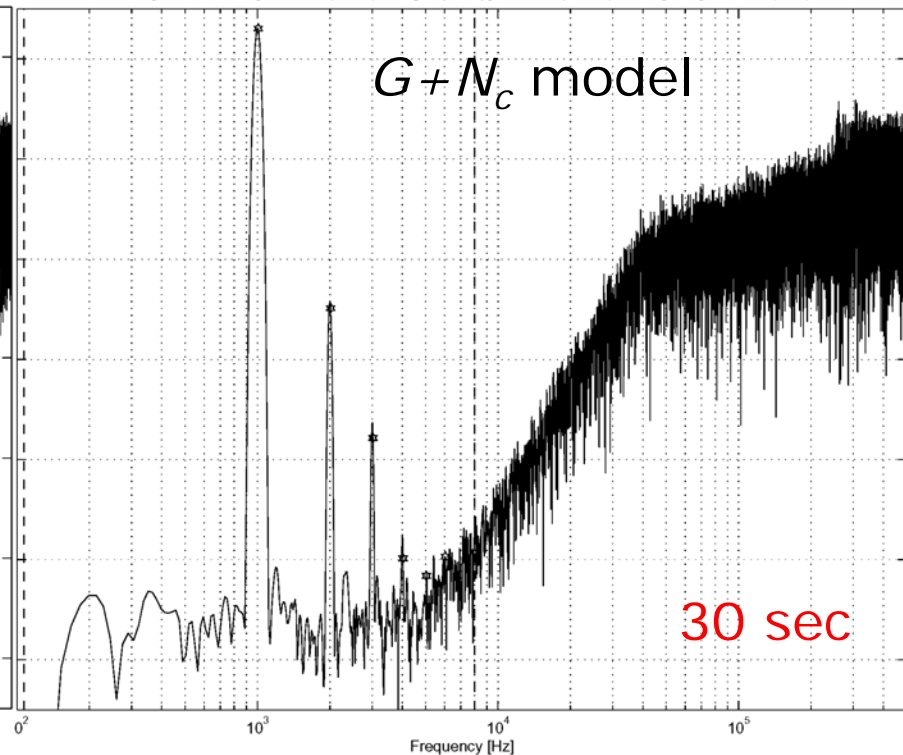
SNR[100Hz,8000Hz]=+69.3dB(11.6b) SDR[2finp,6finp]=+57.8dB(0.13%) SNDR[Total]=+57.5dB(9.6b)

RTZ wave



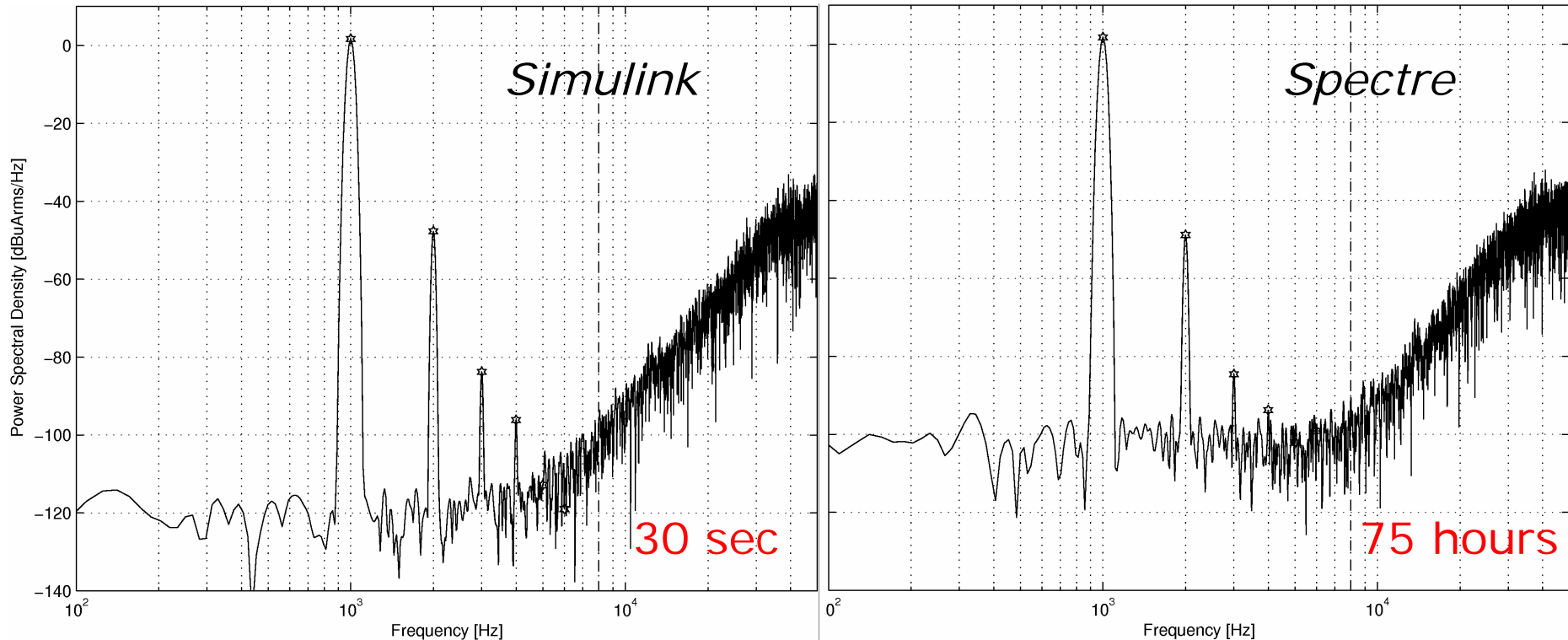
SNR[100Hz,8000Hz]=+68.8dB(11.5b) SDR[2finp,6finp]=+55.8dB(0.16%) SNDR[Total]=+55.6dB(9.3b)

$G+N_c$ model



Electrical vs. High-level simulations

- ▶ Electrical simulation allways needed for model validation
- ▶ Differences on noise floor due to ...
numerical convergence , non-modeled effects



Conclusions

- ▶ Simple, fast and easy to calculate high-level model for feedback DAC on continuous-time modulators $\Sigma\Delta$ presented
- ▶ Simulation speed improved around 10~10000 times
- ▶ Modulator complete performance estimations can be iterated
- ▶ RTZ duty cycle can be dynamically adjusted to work on optimal operation conditions